## **Applied Statistics**

## Assignment #3 and Term paper

## Due February 4th, 2020

# Submit at a box located on the  $5^{th}$  floor (Economic Research Building) by 5pm on February  $4^{th}$  (Tue).

(The box opens during January 14<sup>th</sup> -February 4<sup>th</sup>).

- Assignment #3. Consider the model and the dataset of Exercise 4 in Chapter 5 (Section 5.13). Use WinBUGS to answer the following questions.
  - (1) Estimate posterior means, standard deviations and 95% credible intervals of  $\beta_0$  and  $\beta_1$ .
  - (2) Plot the estimated marginal posterior densities of  $\beta_0$  and  $\beta_1$ .
  - (3) Show your "MCMC output analysis".
    - Show trace plots, and sample autocorrelation functions of  $\beta_0$  and  $\beta_1$ ..
    - Is the sampling algorithm efficient?
    - Does your Markov chain converge?
- 2. Empirical study using Markov chain Monte Carlo method
  - (1) Use real data (do not use simulated data). Where do you get the dataset?
  - (2) Describe your statistical model. What are model parameters?
  - (3) Specify your prior distributions and write the likelihood.
  - (4) Show your "MCMC output analysis"
    - Sample paths (trace plots) of parameters of interest
      - > Explain how you determine the burn-in period
      - > Does your Markov chain converge?
    - Sample autocorrelation functions of parameters of interest
      - ➤ Is your sampling algorithm efficient?
    - Summary statistics of parameters of interest
      - Posterior means, posterior standard deviations, and 95% credible intervals
      - > Plot of the marginal posterior densities
      - > Interpret your MCMC estimation results
  - (5) Sensitivity analysis
    - Check the prior sensitivity. What if you change your prior distributions?
  - (6) Attach your WinBUGS code to the empirical paper.